

FIGURE P8.53

SECTION 8.7 ANGULAR MOMENTUM

54. Each of the following objects has a radius of 0.180 m and a mass of 2.40 kg, and each rotates about an axis through its center (as in Table 8.1) with an angular speed of 35.0 rad/s. Find the magnitude of the angular momentum of each object. (a) a hoop (b) a solid cylinder (c) a solid sphere (d) a hollow spherical shell
55. (a) Calculate the angular momentum of Earth that arises from its spinning motion on its axis, treating Earth as a uniform solid sphere. (b) Calculate the angular momentum of Earth that arises from its orbital motion about the Sun, treating Earth as a point particle.

56. **ecp** A 0.005-kg bullet traveling horizontally with a speed of 1.00×10^3 m/s enters an 18.0-kg door, imbedding itself 10.0 cm from the side opposite the hinges as in Figure P8.56. The 1.00-m-wide door is free to swing on its hinges. (a) Before it hits the door, does the bullet have angular momentum relative to the door's axis of rotation? Explain. (b) Is mechanical energy conserved in this collision? Answer without doing a calculation. (c) At what angular speed does the door swing open immediately after the collision? (The door has the same moment of inertia as a rod with axis at one end.) (d) Calculate the energy of the door-bullet system and determine whether it is less than or equal to the kinetic energy of the bullet before the collision.

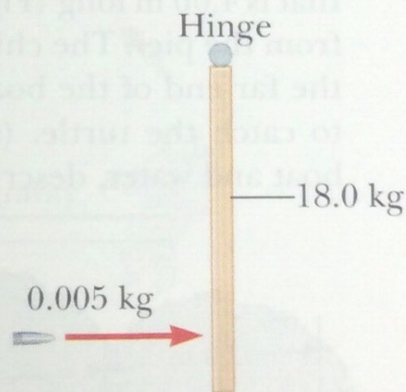
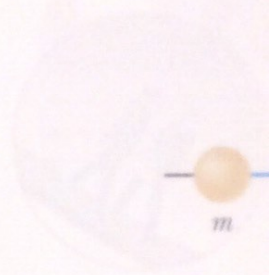


FIGURE P8.56

60. A playground merry-go-round has a moment of inertia of $200 \text{ kg}\cdot\text{m}^2$ and is free to rotate about a frictionless vertical axis through the center. A child of mass 25.0 kg is standing on the merry-go-round at a distance of 1.00 m from the center. The child then pulls in their arms, reducing the radius to 0.500 m. (a) What is the angular speed of the merry-go-round when the child reaches the center? (b) What is the child's angular speed at that time? (c) What is the child's tangential speed at that time?
61. A solid, horizontal cylinder of mass 10.0 kg and length 1.00 m rotates with an angular speed of 100 rad/s about a fixed vertical axis through the center and perpendicular to the length of the cylinder. A lump of putty of mass 0.900 kg is dropped from a height of 1.00 m and sticks to the cylinder at a point 0.900 m from the center. Determine the angular speed of the cylinder immediately after the collision.
62. A student sits on a rotating stool holding two objects. When his arms are extended, the objects are 1.0 m from the axis of rotation. The stool rotates with an angular speed of 1.0 rad/s. The student then pulls the objects in, reducing the moment of inertia of the student and objects to one-half of its initial value. (a) What is the final angular speed of the student and objects? (b) What is the final kinetic energy of the student and objects? (c) What is the change in the kinetic energy of the student and objects?



57. A light rigid rod 1.00 m in length rotates about an axis perpendicular to its length and through its center, as shown in Figure P8.45. Two particles of masses 4.00 kg and 3.00 kg are connected to the ends of the rod. What is the angular momentum of the system if the speed of each particle is 5.00 m/s? (Neglect the rod's mass.)
58. Halley's comet moves about the Sun in an elliptical orbit, with its closest approach to the Sun being 0.59 A.U. and its greatest distance being 35 A.U. (1 A.U. is the Earth-Sun distance). If the comet's speed at closest approach is 54 km/s, what is its speed when it is farthest from the Sun? You may neglect any change in the comet's mass and assume that its angular momentum about the Sun is conserved.
59. The system of small objects shown in Figure P8.59 is rotating at an angular speed of 2.0 rev/s. The objects are connected by light, flexible spokes that can be lengthened or shortened. What is the new angular speed if the spokes are shortened to 0.50 m? (An effect similar to that illustrated in this problem occurred in the early stages of the formation of our galaxy. As the massive cloud of dust and gas that was the source of the stars and planets contracted, an initially small angular speed increased with time.)

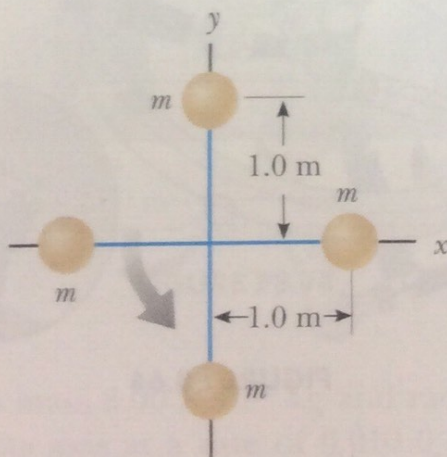


FIGURE P8.59

60. A playground merry-go-round of radius 2.00 m has a moment of inertia $I = 275 \text{ kg} \cdot \text{m}^2$ and is rotating about a frictionless vertical axle. As a child of mass 25.0 kg stands

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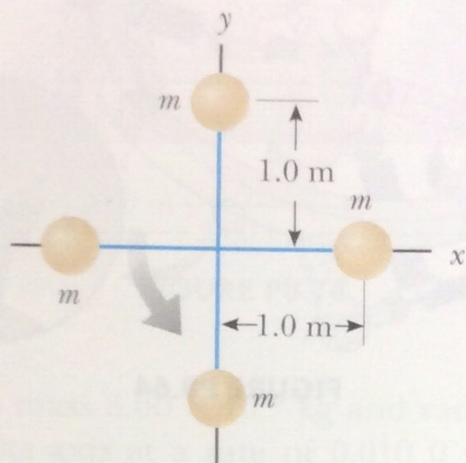


FIGURE P8.59

60. A playground merry-go-round of radius 2.00 m has a moment of inertia $I = 275 \text{ kg} \cdot \text{m}^2$ and is rotating about a frictionless vertical axle. As a child of mass 25.0 kg stands at a distance of 1.00 m from the axle, the system (merry-go-round and child) rotates at the rate of 14.0 rev/min. The child then proceeds to walk toward the edge of the merry-go-round. What is the angular speed of the system when the child reaches the edge?
61. A solid, horizontal cylinder of mass 10.0 kg and radius 1.00 m rotates with an angular speed of 7.00 rad/s about a fixed vertical axis through its center. A 0.250-kg piece of putty is dropped vertically onto the cylinder at a point 0.900 m from the center of rotation and sticks to the cylinder. Determine the final angular speed of the system.
62. A student sits on a rotating stool holding two 3.0-kg objects. When his arms are extended horizontally, the objects are 1.0 m from the axis of rotation and he rotates with an angular speed of 0.75 rad/s. The moment of inertia of the student plus stool is $3.0 \text{ kg} \cdot \text{m}^2$ and is assumed to be constant. The student then pulls in the objects horizontally to 0.30 m from the rotation axis. (a) Find the new angular speed of the student. (b) Find the kinetic energy of the student before and after the objects are pulled in.

63. The puck in Figure P8.63 has a mass of 0.120 kg. Its original distance from the center of rotation is 40.0 cm, and it moves with a speed of 80.0 cm/s. The string is pulled downward 15.0 cm through the hole in the frictionless table. Determine the work done on the puck.
Hint: Consider the change in kinetic energy of the puck.

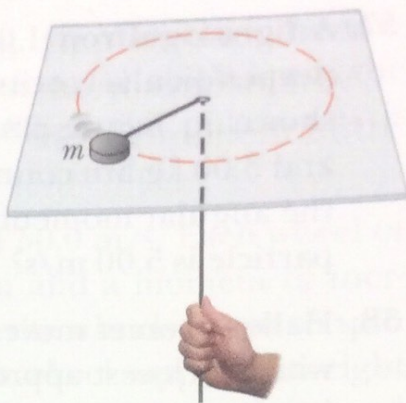


FIGURE P8.63

64. A space station shaped like a giant wheel has a radius of 100 m and a moment of inertia of $5.00 \times 10^8 \text{ kg} \cdot \text{m}^2$. A crew of 150 lives on the rim, and the station is rotating so that the crew experiences an apparent acceleration of $1g$ (Fig. P8.64). When 100 people move to the center of the station for a union meeting, the angular speed changes. What apparent acceleration is experienced by the managers remaining at the rim? Assume the average mass of a crew member is 65.0 kg.

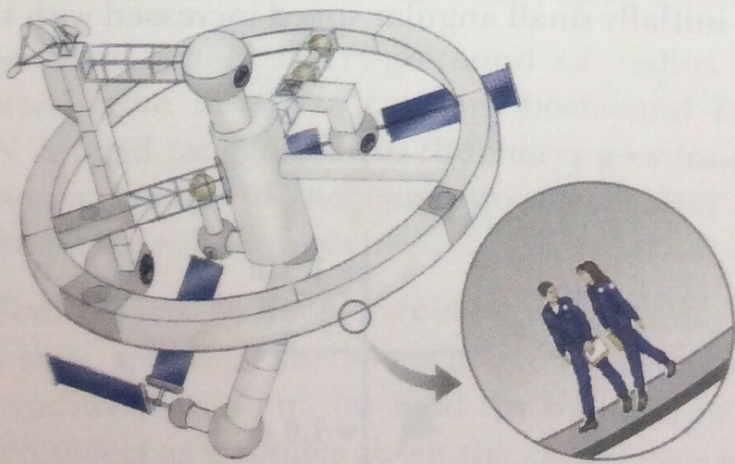


FIGURE P8.64

65. **ecp** A cylinder with moment of inertia I_1 rotates with angular velocity ω_0 about a frictionless vertical axle. A second cylinder, with moment of inertia I_2 , initially not rotating, drops onto the first cylinder (Fig. P8.65).

(b) Calculate the man's moment of inertia and his kinetic energy.

67. A 60.0-kg wheel of radius 2.0 m is free to rotate about its center. The wheel rotates clockwise (a) with an angular speed of 1.5 rad/s and with what angular momentum? (b) How much work is done to bring the turntable to rest?

ADDITIONAL PROBLEMS

68. Figure P8.68 shows a hand pulling a nail on a rotating turntable. The turntable has a moment of inertia of $150 \text{ kg} \cdot \text{m}^2$. (a) What is the force exerted by the hand? (b) What is the force exerted by the turntable on the hand? (c) What is the work done by the hand on the turntable? (d) What is the work done by the turntable on the hand? (e) What is the work done by the turntable on the nail? (f) What is the work done by the nail on the turntable? (g) What is the work done by the nail on the hand? (h) What is the work done by the hand on the nail? (i) What is the work done by the turntable on the nail? (j) What is the work done by the nail on the turntable?

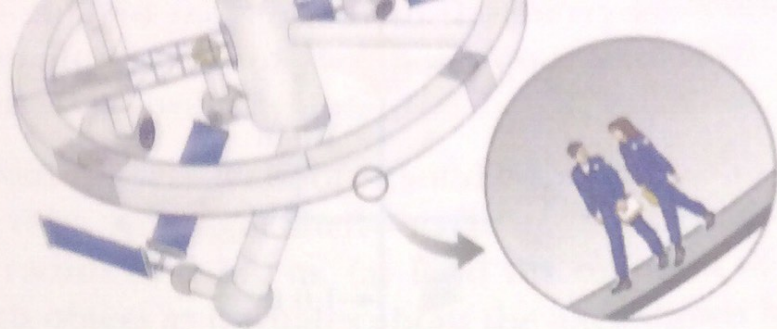


FIGURE P8.64

65. **ecp** A cylinder with moment of inertia I_1 rotates with angular velocity ω_0 about a frictionless vertical axle. A second cylinder, with moment of inertia I_2 , initially not rotating, drops onto the first cylinder (Fig. P8.65). Because the surfaces are rough, the two cylinders eventually reach the same angular speed ω . (a) Calculate ω . (b) Show that kinetic energy is lost in this situation, and calculate the ratio of the final to the initial kinetic energy.

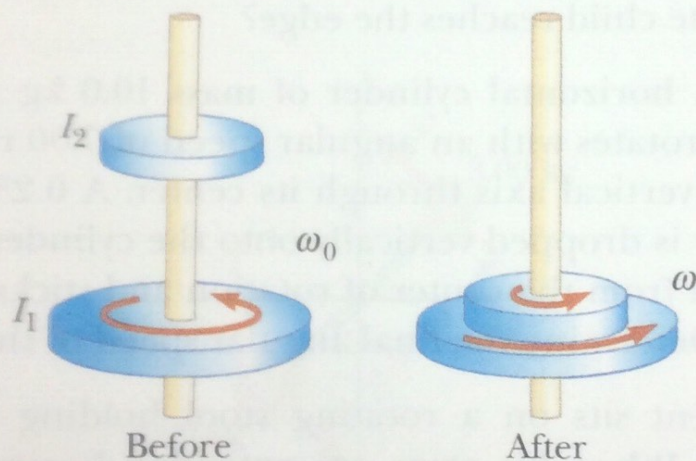
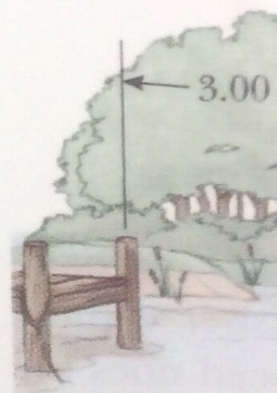


FIGURE P8.65

66. A merry-go-round rotates at the rate of 0.20 rev/s with an 80-kg man standing at a point 2.0 m from the axis of rotation. (a) What is the new angular speed when the man walks to a point 1.0 m from the center? Assume that the merry-go-round is a solid 25-kg cylinder of radius 2.0 m.

69. **ecp** A 40... that is 4.0... from the p... the far en... to catch... boat and



(b) Calculate the change in kinetic energy due to the man's movement. How do you account for this change in kinetic energy?

- 67.** A 60.0-kg woman stands at the rim of a horizontal turntable having a moment of inertia of $500 \text{ kg}\cdot\text{m}^2$ and a radius of 2.00 m. The turntable is initially at rest and is free to rotate about a frictionless, vertical axle through its center. The woman then starts walking around the rim clockwise (as viewed from above the system) at a constant speed of 1.50 m/s relative to Earth. (a) In what direction and with what angular speed does the turntable rotate? (b) How much work does the woman do to set herself and the turntable into motion?

ADDITIONAL PROBLEMS

- 68.** Figure P8.68 shows a clawhammer as it is being used to pull a nail out of a horizontal board. If a force of magnitude 150 N is exerted horizontally as shown, find (a) the force exerted by the hammer claws on the nail and (b) the force exerted by the surface at the point of contact with the hammer head. Assume that the force the hammer exerts on the nail is parallel to the nail and perpen-