### **Projectile Motion (Intro) PhET Simulations Lab**

#### Introduction:

Projectiles travel with two components of motion, X any Y. The acceleration and velocity in the Y direction is independent of the acceleration (if any) and velocity in the X direction. In this module, you will investigate the motion of a simple projectile. Realize that while gravity (acceleration) acts on the projectile in the \_\_\_\_\_\_ direction, it does not affect the velocity of the projectile in the \_\_\_\_\_\_ direction.

### Procedure:

# (we will be ignoring air resistance during this lab)

- Run the PhET Simulations  $\rightarrow$  Play  $\rightarrow$  Motion  $\rightarrow$  Projectile Motion Run Now!
- The cannon can be moved to add or remove initial Y position and X position.
- The cannon can be pivoted to change the firing angle,  $\theta$ .
- The tape measure can be moved and dragged to measure range to target.
- To fire the cannon, Fire
- To erase the projectile's path, **Erase**.

## Be sure air resistance is off and spend some time firing various projectiles.

- Set the initial speed to a value between 10-15m/s. Choose your favorite projectile.
- Find the range of the projectile at various angles.  $\theta = 30$  Range (dx) = \_\_\_\_ m  $\theta = 70$  Range (dx) = \_\_\_\_ m  $\theta = 40$  Range (dx) = \_\_\_\_ m  $\theta = 80$  Range (dx) = \_\_\_\_ m  $\theta = 50$  Range (dx) = \_\_\_\_ m  $Add \text{ two} = Range (dx) = ____ m$   $\theta = 60$  Range (dx) = \_\_\_\_ m  $\theta = Range (dx) = ____ m$ 
  - Measure the distance from the cannon to the target using the tape measure.
  - Move the target to 21.0 m from the cannon. Attempt to hit the target with three different angles by changing the firing angle and initial velocity.



## VERY IMPORTANT

A projectile's velocity (v) has an X component (v<sub>x</sub>) and a Y component (v<sub>y</sub>). The X component (v<sub>x</sub>) is found by multiplying the magnitude of the velocity by the *cosine* of the angle,  $\theta$ .

Similarity, the Y component of velocity is found by multiplying the magnitude of the velocity by the *sine* of the angle,  $\theta$ .

 $v_y = v \sin \theta$ 

 $v_x = v \cos \theta$ 

So, a projectile fired at **20 m/s** at **65°** has an X-velocity of  $v_x = 20\cos 65$  or **8.5** m/s.

The projectile would have a Y-velocity of  $v_y = 20 \sin 65$  or **18** m/s.

So, the projectile would fire <u>as far as one fired horizontally at 8.5 m/s</u> and <u>as high as one fired straight</u> <u>up at 18 m/s</u>.

A projectile fired at 30 degrees with a velocity of 15 m/s would have an x-velocity component of \_\_\_\_\_\_ m/s and a y-velocity component of \_\_\_\_\_\_ m/s.



Calculate the components of the following projectile's velocities:

- 1.  $v = 35 \text{ m/s } \theta = 15^{\circ} v_x = \___ v_y = \___ v_y$
- We can reverse the process and combine the two components of velocity back into one velocity fired at an angle.
- ★ The magnitude of velocity is found using the Pythagorean Theorem with  $v_x$  and  $v_y$  as the legs of a right triangle. For instance, the velocity of a projectile with an x-component of 7.2 and a y-component of 4.8 is  $\sqrt{7.2^2 + 4.8^2} = 8.7 \text{ m/s}$ .
- ★ The angle above the horizontal is found using the inverse tangent (tan<sup>-1</sup>) of the legs  $v_y/v_x$ . For instance, the angle of the projectile described above would be  $tan^{-1}(\frac{4.8}{7.2}) = 34^{\circ}$ .

Calculate the velocity magnitude and angle of the projectiles listed below:

 7.  $v_x = 5.6 \ v_y = 6.4 \ v = \____ \ \theta = \_____ \ \theta = \____ \ \theta = \_$ 

# **Conclusion Questions:**

- 1. Without air resistance, the piano travels further / the same distance as the football. (circle)
- 2. This is due to the fact that velocity in the X-direction *increases / is constant / decreases* as projectiles travel.
- 3. The Y-component of velocity increases / is constant / decreases as projectiles travel.
- 4. The answers to #2 and #3 are due to the fact that gravity acts *only in the Y / both the X any Y* direction.
- 5. The path of a projectile is a *linear curve / round curve / parabolic curve*.
- 6. This is due to the fact that the time component in the free fall equation (dy) is \_\_\_\_\_\_.
- 7. Without air resistance, maximum range of a projectile is obtained with an angle of \_\_\_\_\_\_.
- 8. The same range can be obtained with angles of \_\_\_\_\_\_ and \_\_\_\_\_.
- 10. A projectile with a horizontal component of 13 m/s and a vertical component of 18 m/s would have an overall velocity of \_\_\_\_\_\_ m/s at an angle of \_\_\_\_\_\_ above the horizontal.