

Translational

$$\text{Work} = F \cdot d \cdot \cos \angle \frac{F}{d}$$

$$\text{Power} = \frac{\text{work}}{t} = F \cdot v \cdot \cos \angle \frac{F}{v}$$

$$K_{\text{translational}} = \frac{1}{2} m v^2$$

Linear Momentum $P = m \cdot v$

P is constant or conserved if $F_{\text{net}} = 0$

$$\text{Impulse} = F_{\text{ave}} \cdot \Delta t$$

Rotational

$$\text{Work} = \tau \cdot \Delta \theta \cdot \cos \angle \frac{\tau}{\Delta \theta}$$

$$\text{Power} = \tau \cdot \omega \cdot \cos \angle \frac{\tau}{\omega}$$

$$K_{\text{rotational}} = \frac{1}{2} I \omega^2$$

Angular Momentum $L = I \omega$

L is constant or conserved if $\tau_{\text{net}} = 0$

$$\text{Angular Impulse} = \tau_{\text{ave}} \cdot \Delta t$$



I : rotational inertia or moment of inertia

Translational motion

$$K_{\text{trans.}} = \frac{1}{2} m v^2$$

Rotational motion

$$K_{\text{rot.}} = \frac{1}{2} I \omega^2$$

equal!

$$\frac{1}{2} m v^2 = \frac{1}{2} I \omega^2$$

$$m v^2 = I \omega^2$$

$$m (r \omega)^2 = I \omega^2$$

$$m r^2 \cancel{\omega^2} = I \cancel{\omega^2}$$

$$m r^2 = I$$

Inertia for pt. mass

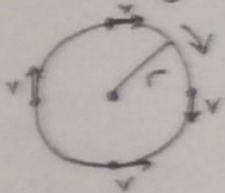
$$I = m r^2$$

depends on the location of the mass and how much mass it has.

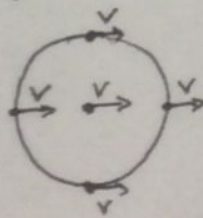
The point mass should have the same amount of energy regardless whether we treat it as having rotational or translational energy.

' r ' is the distance between the mass and the axis.

Rolling without slipping:



rotate about fixed axis
 $\text{dist.} = r \cdot \Delta \theta$
 $\text{spd} = r \omega$
 $a_T = r \alpha$



translational motion of center axis
 $\text{dist.} = r \cdot \Delta \theta$
 $\text{vel. } v = r \omega$
 $a = r \alpha$

