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## PhET 2D Motion and Vectors Simulations Lab $r v s d$ 8/2010

## Introduction:

A vector quantity is one that has both a magnitude and a direction. For instance, your car's velocity vector will have a magnitude ( $24 \mathrm{~m} / \mathrm{s}$ ) and a direction (northeast or 45 degrees). These simulations will illustrate how vectors are made of X and Y components, how two vectors can be added to produce a resulting vector, and how the acceleration vector affects the velocity vector in two-dimensional motion.


Ladybug Motion 2D

Part I: Vector Simulation: Play With Sims $\rightarrow$ Physics $\rightarrow$ Motion $\rightarrow$ LadyBug 2D Motion Run Now!

1. Click Manual. Drag the bug around with your mouse and notice the actions of the two vectors. Spend some time investigating the vectors. Which vector is velocity? $\qquad$ and which is acceleration? $\qquad$

## 2. Be sure everyone in the lab group does ALL these exercises.

3. Describe the direction of the red vector (in relation to the green vector) when the bug sped up.

Trace
5. Click Circular. Observe the bug's motion. Where must the acceleration vector be (in relation to the velocity vector) to turn the bug?
6. Click Ellipse. Observe the bug moving like a car on a racetrack (in an oval). What must a car/runner do in order to turn?
$\qquad$
7. Now....use the Remote Control ${ }_{\text {area }}$ to manually move the bug by controlling its position, velocity, and acceleration. Try to make the letter " C " three times using position, then velocity, then acceleration.

8. Try to trace other letters, such as "O","D","S","J","P". Challenge your labmates! What can you trace using acceleration?

## Part II: Vector Addition Simulation: Play With Sims $\rightarrow$ Math $\rightarrow$ Vector Addition Run Now!

Place two vectors in the work area. Change their direction and magnitude be dragging the heads of the arrows representing each vector. Click show sum to view the resultant (sum) of the two vectors. You may click the Styles to show the $X$ and $Y$ components.

Click on one vector and fill in the boxes:


Click on another vector and fill in the boxes:



Vector Addition
Click the resultant vector and fill in:


Repeat with two different vectors: Vectors 1 and 2

$\theta \square$
$\mathrm{R}_{\mathrm{x}}$ $\square$ $\mathbf{R}_{\mathbf{y}} \square$

## The Resultant Vector



## Part III: Calculating Resultant Vectors: ${ }^{* * *}$ GRADED***

Find the mathematical sum of each set of vectors below (with a calculator).
After you have calculated, recreate (as closely as possible) the vectors in the simulation to check your work.

## Vector Components and Vector Addition Review:

- To add vectors, break each vector into its X an Y components by calculating $M \cos \theta=X$ and $M \sin \theta=Y$. The components CAN BE NEGATIVE ( $-\mathrm{x},-\mathrm{y}$ )
- The resultant vector's X and Y components are the sum of the X and Y components of each vector: $X_{r}=X_{1}+X_{2}$
- The resultant vector's magnitude $\boldsymbol{M}$ or $|\mathbf{R}|$ is found using the Pythagorean theorem using $X_{r}$ and $Y_{r}$ as the legs of a right triangle, where the hypotenuse is the magnitude.
- The angle $\boldsymbol{\theta}$ of the resultant vector is found with the inverse tangent $\left(\boldsymbol{\operatorname { t a n }}^{-1}\right)$ of the $X_{r}$ and $Y_{r}$ components.

Fill in all available boxes - exact, graded answers will come from calculations, use the sim to check your work


| $M$ | angle, $\theta$ | $X_{1}$ | $Y_{1}$ |
| :---: | :---: | :---: | :---: |
| 6.0 | 35 |  |  |

Vector 2

| $M$ | angle, $\theta$ | $X_{2}$ | $Y_{2}$ |
| :---: | :---: | :---: | :---: |
| 2.5 | 20. |  |  |

Resultant of adding vector 1 and vector 2 components

| $\mathrm{Mr}_{r}$ | $\theta_{\mathrm{r}}$ | $\mathrm{X}_{\mathrm{r}}$ | $\mathrm{Y}_{\mathrm{r}}$ |
| :---: | :---: | :---: | :---: |
|  |  |  |  |

## \#2

Vector 1

| $M$ | negative angles - be careful |  |  |
| :---: | :---: | :---: | :---: |
| 1.8 | 15 |  |  |
| angle, $\theta$ | $X_{1}$ | $Y_{1}$ |  |
| Vector 2 |  |  |  |
| $M$ | angle, $\theta$ | $X_{2}$ | $Y_{2}$ |
| 7.0 | -25 |  |  |

## Resultant

| $\mathrm{M}_{\mathrm{r}}$ | $\theta_{\mathrm{r}}$ | $\mathrm{X}_{\mathrm{r}}$ | $\mathrm{Y}_{\mathrm{r}}$ |
| :---: | :---: | :---: | :---: |
|  |  |  |  |

Vector 1

| $M$ | angle, $\theta$ | $X_{1}$ | $Y_{1}$ |
| :---: | :---: | :---: | :---: |
|  |  | 3.5 | 2.5 |

Vector 2

| $M$ | angle, $\theta$ | $X_{2}$ | $Y_{2}$ |
| :---: | :---: | :---: | :---: |
|  |  | 4.0 | 6.0 |

## Resultant

| $\mathrm{Mr}^{2}$ | $\theta_{\mathrm{r}}$ | $\mathrm{X}_{\mathrm{r}}$ | $\mathrm{Y}_{\mathrm{r}}$ |
| :---: | :---: | :---: | :---: |
|  |  |  |  |
|  |  |  |  |

\#4
Vector 1

| $M$ | angle, $\theta$ | $X_{1}$ | $Y_{1}$ |
| :---: | :---: | :---: | :---: |
|  | 70 | 4.7 |  |

Vector 2

| $M$ | angle, $\theta$ | $X_{2}$ | $Y_{2}$ |
| :---: | :---: | :---: | :---: |
|  | -15 |  | -2.0 |

Resultant

| $M_{r}$ | $\theta_{r}$ | $X_{r}$ | $Y_{r}$ |
| :---: | :---: | :---: | :---: |
|  |  | 12.1 | 10.8 |

## 2D Motion Conclusion Questions:

1. The red vector represented $\qquad$ and the green represented $\qquad$ .
2. When the acceleration vector was in the same direction as the velocity vector, the object slowed down / sped up.
3. When the acceleration vector was in the opposite direction as the velocity vector, the object slowed down / sped up.
4. Turning requires the acceleration vector to be directed where? $\qquad$
5. Imagine tracing the letter "J". As the ladybug is travelling down, it must turn to make the hook. In what direction must the acceleration vector point to move the velocity vector (from down) and trace the hook? $\qquad$
